

EVALUATION OF STIFFNESS DEGRADATION CURVES FROM IN SITU TESTS IN VARIOUS SOIL TYPES

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Increasingly complex design systems require an individual approach when determining the necessary design parameters. As soils are characterized by strong strain-dependent nonlinearity, test methods used to characterize the subsoil should be carefully selected, in terms of their "sensitivity" as well as suitability for the analyzed type of problem. When direct measurements are not available, while design calculation models require specific parameters, indirect parameter estimation may be used. This approach requires calibration and validation of empirical correlations, based on well documented database of tests and case studies. One of the parameters often used, when analyzing soil-structure interaction problems, is the shear stiffness of the soil and its strain-dependent degradation. The aim of the article is to present the procedure for description and evaluation of soil stiffness based on field tests (CPTU, DMT and SDMT) and a large number of reference curves obtained from laboratory tests (TRX) for selected soil types. On the basis of the given algorithm, it is possible to obtain a stiffness module G_0 value at any level of deformation, based on in-situ tests.

Keywords: soil stiffness, in situ tests, reference stiffness degradation curve, seismic dilatometer; overconsolidated soils.

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1. INTRODUCTION

Design of foundations and geotechnical structures requires obtaining proper parameters characterizing the subsoil [4], [11], [29], [39], [45], [55]. These parameters should be sufficiently reliable, therefore, obtained using methods that were properly validated or calibrated in local conditions [5], [11], [17], [51], [60]. The field testing methods have a very important role to play in this regard [24], [51]. Significant progress has been made in recent decades in regard to the equipment, automation, advancement in measurement registration and interpretation. As designers often use semi-empirical approaches, the results of these tests are often expected in geotechnical documentations. In recent years, new developments are mostly focused on implementation of geophysics in the measurements in order to measure shear wave velocities in the subsoil [14], [19], [35]. This offers a chance to make an estimate concerning the stiffness of the subsoil in the entire range of strain-dependent stiffness degradation. In order to ensure the safety and rational design for civil engineering structures, proper estimation of geotechnical parameters is necessary when analyzing soil-structure interaction [54]. When quantitatively estimating the value of deformation modulus of the soil, the choice should depend on the expected behavior of the structure. It means that this modulus should correspond to the stress-strain range of particular structure together with possible dynamic loads [3], [16], [35]. The discovery that the deformation modulus is highly non-linear in small deformations range (10^{-6} – 10^{-3} %) was a large step forward in soil mechanics [3], [9], [25], [36]. Testing methods that allow to determine the values of modulus in this range are classified as advanced, where often the measurements of seismic waves are used. The fact that these methods of stiffness parameters determination are useful was confirmed by back analysis on constructed structures (for example: deep excavations) [4], [16], [38], [39], [45], [55] where moduli from geophysical methods were higher than the values provided in standards or those determined by classical methods. Soil stiffness, at small strains, is a relevant parameter in solving boundary value problems such as: response of soil deposits to earthquakes or dynamic interaction between soils and foundations [24]. However, it has been pointed out by many researchers that the strain level which often occurs in geotechnical problems is quite small even under the static loading condition and in the case of conventional foundations [25].

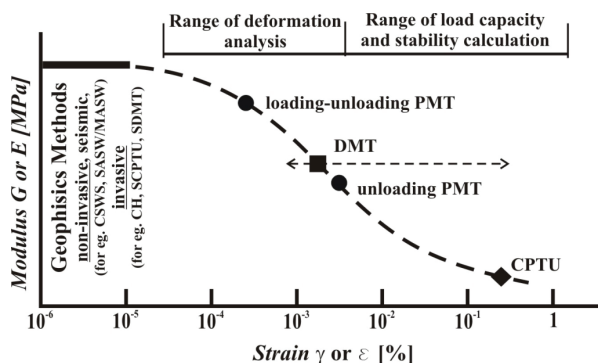


Fig. 1. Strain-dependent non-linearity of shear stiffness modulus in light of strain-levels associated with different structure-types and testing methods (modified [19] after [1]).

In complex loading conditions, when the subsoil can work at different strain-levels, the behavior over the entire stiffness degradation curve has to be obtained [3], [9], [16], [29], [58]. The main problem is associated with the characterization of degradation curve during shearing (from τ - γ for shear modulus G or σ - ε for deformation modulus E). In the analysis of soil behavior, the term “soil stiffness” is often used while assuming deformations in the elastic range (pseudo-elastic), resulting from static loading, and it is measured as shear stiffness modulus G_0 , or represented also as initial stiffness modulus E_0 . These parameters can be estimated based on measured shear wave velocity V_s . The derived parameters E_0 and G_0 are estimated as:

$$(1.1) \quad E_0 = 2\rho V_s^2(1 + \nu)$$

$$(1.2) \quad G_0 = \rho V_s^2$$

where:

V_s – shear wave velocity, ν – Poisson’s coefficient, ρ – bulk density .

Shear modulus depends on a number of factors, which were described in the equation presented by Hardin & Black [after 21]:

$$(1.3) \quad G_0 = f(\sigma'_0, e, S, C, A, F, T, \theta, K)$$

where:

σ'_0 – effective horizontal pressure, e – void ratio, S – saturation ratio, C – size-mineralogy characteristic, A – amplitude, F – frequency, T – time effects, θ – soil structure, T – temperature.

In practice, not all of these parameters are used when estimating the shear stiffness modulus G_0 as not all of them have the same impact on the value of shear wave velocity. The most important factors taken into account in most commonly used expressions are void ratio and effective stress, related also to stress history [21]:

$$(1.4) \quad G_0 = A(T)F(e)\sigma'_n$$

$$(1.5) \quad G_0 = S(T)F(E)\sigma'_n OCR_k$$

where:

σ'_n – effective normal pressure, OCR – over consolidated void ratio, E – deformation modulus,

The equations were proposed by Hardin & Black and Hardin [21]. To evaluate the small strain shear modulus, the following most common empirical correlations, based on penetration tests results or laboratory results available in literature for various type of soils, are shown below:

a) Hardin (1978) [21]

$$(1.6) \quad G_0 = 6250.3 + 0.7e^2 \cdot OCR_k \cdot (\sigma'_0 p_a)^{0.5}$$

where:

k – empirical value, p_a – reference pressure (98.1 kPa)

b) Hryciw (1990) [22]

$$(1.7) \quad G_0 = \frac{530}{(\sigma'_v/p_a)^{0.25}} \frac{\gamma_D/\gamma_w - 1}{2.7 - \gamma_D/\gamma_w} K_0^{0.25} \cdot (\sigma'_v \cdot p_a)^{0.5}$$

where:

p_a – reference pressure (1 bar), γ_D and K_0 are respectively the unit weight and the coefficient of earth pressure at rest, (as inferred from SDMT results according to Marchetti [33]).

c) Mayne and Rix [37]

$$(1.8) \quad G_0 = \frac{406 \cdot q_c^{0.696}}{e^{1.13}}$$

where:

G_0 , σ'_v and p_a are expressed in the same units; e - void ratio (this equation is applicable to clay deposits only);

d) Jamiolkowski et al. (1995) [24]

$$(1.9) \quad G_0 = \frac{600 \cdot \sigma'_m{}^{0.5} p_a^{0.5}}{e^{1.3}}$$

where:

$\sigma'_m = (\sigma'_v + 2 \cdot \sigma'_h)/3$; $p_a = 1$ bar is a reference pressure; G_0 , σ'_m and p_a are expressed in the same units (this equation is applicable to clay and reconstituted sands)

e) Aoki et al. (1997) [4]

$$(1.10) \quad G_0 = 1034 \frac{(2.97-e)^2}{1+e} \sigma_v'^{0.59} \quad \text{for non-cohesive soils}$$

$$(1.11) \quad G_0 = 804 \frac{(2.17-e)^2}{1+e} \sigma_v'^{0.26} \quad \text{for cohesive soils}$$

The benefits of accounting for non-linearity of this stress-strain relationship has led to the need of measuring soil stiffness over a range of small deformations (10^{-6} – 10^{-3}) and utilization of many methods for this purpose [3]. As described by (e.g. Mayne [37], Clayton [9]), several in-situ and laboratory test methods are employed to determine the initial shear modulus G_0 (from the shear wave velocity, V_s): Down-Hole (DH) and Cross-Hole (CH) seismic methods, Seismic Dilatometer Test (SDMT) and Seismic Cone Penetration Tests (SCPT), Spectral Analysis of Surface Waves (SASW), Bender Elements Test (BET), Resonance Column (RC). The Dilatometer test (DMT), Pressuremeter Test (PMT), Triaxial Test (TRX), Oedometer test (OET) are also performed to allow assessment of the stiffness of soils at moderate to large strains. Therefore, non-linear behavior of the soil can be determined by many in-situ and laboratory tests. However, to get the shape of this curve it is necessary to make more detailed investigation (in situ and laboratory tests). However such tests are sophisticated and expensive (due to the cost of taking good quality samples, and cost of necessary equipment). It

is therefore of interest to investigate if in-situ tests can be used to measure G - γ stiffness-degradation curves.

This paper focuses on the seismic dilatometer test (SDMT) where the G - γ curve is derived from the “initial elastic modulus” G_0 based on the shear wave velocity V_s , and a “working strain modulus” (G_{DMT}) corresponding to the Marchetti [32] constrained modulus M_{DMT} . The seismic dilatometer (SDMT) is the combination of the mechanical flat dilatometer (DMT), introduced by Marchetti, with a seismic module for measuring the shear wave velocity V_s . From V_s , the small strain shear modulus G_0 may be determined using the theory of elasticity Eq. (1.2). Marchetti et al. [33] first proposed the possible use of the SDMT for deriving in situ soil stiffness variations with strain level (G -curves or similar). A challenging issue, which the scientific community has focused on in the last decade (e.g. [33], [1], [2], [23]), concerns the possibility of assessing the in situ degradation curves of soil stiffness with shear strain (G - γ curves), based essentially on the G_0 and G_{DMT} experimental data alone. This approach has proven applicable to different soil types, as shown by Amoroso et al. [2]. However, limited data are available as to ascertain the reliability of this procedure for soft materials, especially for organic soils.

In short, in this procedure, some curves could be tentatively constructed by fitting “reference typical-shape” laboratory G -curves through two points, both obtained by SDMT: First point - the initial small strain modulus G_0 , and second point - a working strain modulus G_{DMT} . To locate the second point on the G -curve it is necessary to know, at least approximately, the shear strain corresponding to G_{DMT} . Researches classified the DMT within the group of methods of measurement of soil deformation characteristics involving an intermediate level of strain (0.01-1%) – fig. 1. As suggested by Marchetti et al. [33], [34], a working strain shear modulus G_{DMT} can be derived from the constrained modulus M_{DMT} provided by the usual DMT interpretation [32]. As a first approximation, by referring to linear elasticity:

$$(1.12) \quad G_{DMT} = \frac{1-2\nu}{2(1-\nu)} M_{DMT}$$

The above tentative method is heavily founded on the assumption that M_{DMT} is a reasonable estimate of the working strain modulus [34], [2].

The present paper aims to provide some recommendations for the interpretation of the results from in situ tests commonly used in Polish practice (CPTU, DMT, SDMT). It presents some issues concerning the practical application of field test results obtained mainly using flat dilatometer by Marchetti [32]. The data collected so far allowed to conduct research in the field of determination of

regional relationships between in situ methods [60], [17], including the presentation of practical applications of results obtained with the dilatometer (DMT/SDMT).

This paper illustrates the use of in situ tests, as indirect CPTU and DMT or direct SDMT, to assess the in situ degradation of stiffness at various test sites, where both SDMT data and "reference" stiffness degradation curves from laboratory tests were available. In this case, an advance triaxial apparatus with bender elements and local (on sample) displacements transducers was used as one of the preferred laboratory methods for obtaining the stiffness parameters of the soil.

2. METHODS AND MATERIAL

The correlations between sounding results and geotechnical parameters require regional determination or adaptation for local conditions [11], [17], [40], [60]. Additional difficulties are associated with many other factors that have an influence on the soil behaviour and which are still impossible to measure, or their measurements are not reliable enough. The results from new types of static probes with piezocone (CPTU) or flat dilatometer of Marchetti type (DMT) obtained by foreign researchers refer to local soils and very often may not be applicable directly for Polish soil conditions. Some institutions in Poland have conducted intensive research on interpretation methods of CPTU and DMT results for determination of geotechnical parameters (ϕ' , c_u/s_u , E_{cod}) [5], [6], [15], [17], [26], [27], [30], [40-42], [46-47], [61].

Building Research Institute has extensive experience concerning in situ soil investigations by means of cone penetration test and dilatometer test. The huge number of data points, including different types of soils for different types of construction, has been collected. In the research project [48] the new results were added to the database and statistical analysis was conducted. Wherever it was possible, the modulus obtained from in situ tests was compared to values from back-analysis of settlements measurements. The correlations are based on the results from more than 30 test sites and for different types of soils commonly encountered in Poland. Each test site was considered as a node, consisting of CPTU profile, DMT profile, geological profile, and settlement data [48], [60]. In total, approx. 1700 meters of test profiles were analysed. After extreme values were eliminated, the data was divided into litho-genetic groups from different test sites. When analysing the sounding data with resolution of 20 cm (DMT), for specific litho-genetic types, data sets of 450 to 1500 data points were obtained. The selected profiles consisted of layers with various properties, lithology and origin, were classified according to the Soil Behaviour Type (SBT) classification rule of Robertson [49], [50].

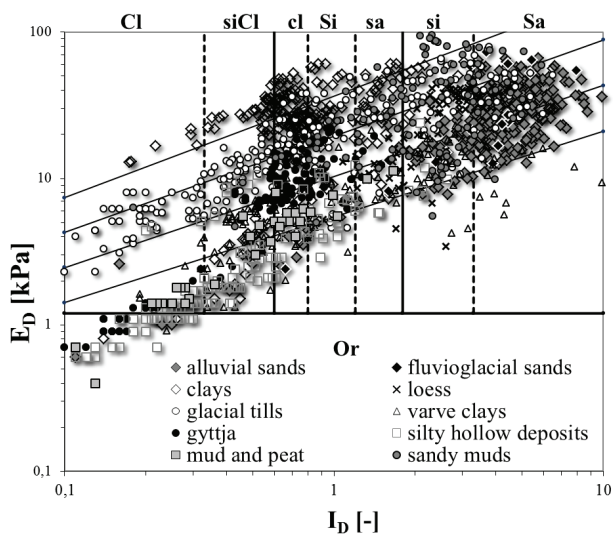


Fig. 2. All results for different test sites for analysed soils plotted on Marchetti's classification nomogram.

These were Miocene-Pliocene clays of Poznań formation (OC), Pleistocene Varve clays (~NC), Pleistocene tills of Warta and Odra glacial period (OC), Pleistocene (Eemian interglacial) limnic soil – Gyttja (OC), young Holocene Alluvial soil - soft silty clay (NC) and alluvial NC deposits of River beds – alluvial sands, fluvioglacial OC deposits – fluvioglacial sands, eolian NC deposits – loess, silty hollow deposits NC, OC – silty sands, silty tills and silts, and young Holocene Alluvial - organic NC deposits – mud (alluvium silt) and peat - fig. 2.

2.1. CALIBRATION OF DMT

The Marchetti flat dilatometer is a device dedicated for determination of deformation parameters of soils. This is supported by the specificity of measurement itself [32]. Expansion of a steel membrane in the soil is a controlled displacement test, i.e. measurement of pressure at desired displacement. This allows for estimating the deformation modulus directly in the soil (in situ) which is the basis for determination of displacements of the designed structure. Worldwide experience [34], [43] [57] indicates that DMT is highly useful in determination of soil deformation moduli. This method is reliable, provided that it is calibrated and validated (by other methods) in local conditions. In this case, the best method is to compare the settlement values measured at given structures or performance of test loads against the settlement values obtained from DMT [43].

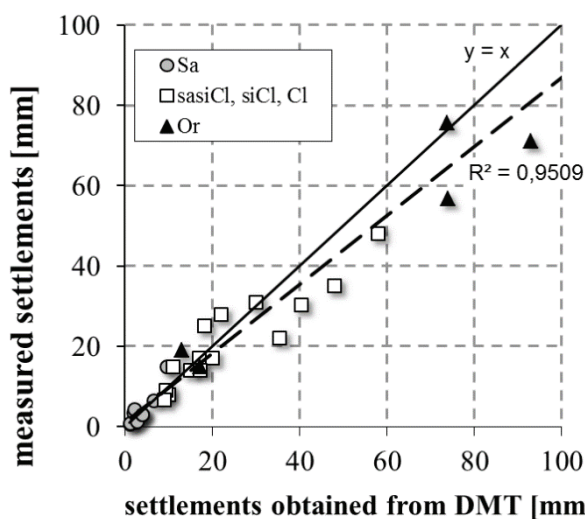


Fig. 3. DMT calibration curve obtained for Polish ground conditions [upgrade from 15]

Acquired experience, in regard to settlement prediction based on DMT, generally confirms the validity of the used equations. Estimated values of moduli, which can be used for settlement prediction, for typical mineral soils, are in line with values obtained from back-analysis of real structures. Fig. 3 shows comparison of settlement values measured at the structures with respect to those obtained by dilatometer data and observations (28 structures) [15]. It should be added that the given set of buildings was limited to structures with shallow foundation. For the purpose of evaluation and forecasting settlement, the dilatometer is a well-calibrated device for typical structures. In the cases of founding on very soft and organic soils, in which the quality of drilling and collected samples is often insufficient, only in situ probing allows for obtaining reliable parameters for design calculations.

2.2 LOCAL CORRELATION OF CPTU/DMT PROBES

Currently, cone penetration tests are very common due to the availability of the equipment. The interpretation of obtained measured parameters (cone resistance, sleeve friction, pore pressure) requires the use of correlations to derive geotechnical parameters. When DMT tests cannot be conducted to obtain in situ degradation curve, but data from CPT are available, local correlations have

2.3 SHEAR MODULUS FROM SDMT

Currently, apart from the standard DMT test, the tests involving geophysical measurements with a dilatometer with a seismic sensor (SDMT) have been often performed. More information on the procedure itself and factors affecting the reliability of obtained results can be found in [33] and [18], [19]. These tests allow for determination of the soil rigidity profile as a function of shear modulus (G_0) by measuring the propagation velocity of a transverse wave (V_s). Due to sufficient experiences of testing with the use of DMT and SDMT, correlations were established, which may be useful when direct seismic measurements are not available. Below, three basic relationships established by Marchetti et al. [33], [34], are presented:

$$(2.1) \quad G_0 = M_{DMT} \cdot 26.177 \cdot K_D^{-1.0066} \text{ for clayed soils}$$

$$(2.2) \quad G_0 = M_{DMT} \cdot 15.686 \cdot K_D^{-0.921} \text{ for silty soils}$$

$$(2.3) \quad G_0 = M_{DMT} \cdot 4.5613 \cdot K_D^{-0.7967} \text{ for sandy soils}$$

where:

M_{DMT} – dilatometer modulus [MPa], K_D – coefficient of horizontal stress [-]

Equations by Marchetti et al. [34] were based on a large spectrum of test results from 34 test locations, where 2000 parameter values were obtained. The examples of local correlations (especially for organic soils), based on the formula presented by Marchetti, are presented below:

f) Rabarijoely (2008) [46]

$$(2.4) \quad G_0 = 2.98 \cdot M_{DMT} \cdot K_D^{-1.2} \text{ for organic soils}$$

g) Młynarek et al. (2013) [40]

$$(2.5) \quad G_0 = 49.97 \cdot M_{CPTU} \cdot K_D^{-1.0} \text{ for sands}$$

$$(2.6) \quad G_0 = 12.35 \cdot M_{CPTU} \cdot OCR^{0.13} \text{ for organic soils}$$

In Poland, some other attempts of regional correlations have already been carried out for organic soil and soft clays by Młynarek et al. [42], Lechowicz et al. [26]. These Authors, for example, define a specific correlation between the Dilatometer Modulus E_d and the Young modulus at 0.1 % level of strain. Similarly, the results from SDMT were used to obtain correlation relationships for the tested soils at the described test sites.

2.4. REFERENCE LABORATORY TEST

For laboratory investigation of elastic deformation characteristics of soils in the range of small strains, with the use of shear wave velocity measurements, the Bender Element Test (BET) was used. This test is often conducted in the triaxial apparatus cell, with the use of piezoelements. Generated and received S- and P-waves allow for estimating the Poisson's coefficient and the initial deformation modulus E_0 of the tested soil. More details about this equipment and technical information were presented in [7], [12], [62].

In this paper, only the results for natural cohesive soils are presented, namely, glacial tills from northern and central Poland and Neogene clays (tab. 2). A total of about 130 samples were taken from the investigation sites for laboratory tests. The tests were carried out using triaxial testing devices. The tests were conducted on undisturbed soil samples, either 70 mm in diameter and the height of 140 mm, or the diameter of 38 mm and the height of 75 mm. The samples were saturated with an automatic pressure control algorithm, until B coefficient reached a value greater than 0.95. After the saturation phase, the isotropic consolidation stage was carried out, followed by the S-wave transition measurements with bender element tests (BET) together with the use of local displacement transducers. In the case of 38 mm diameter samples, both the shear wave and the compressional wave (P-wave) velocities were measured.

Due to the height of the samples, expected range of wave velocities, as well as the need to minimize „near field” effects, the procedure presented by Camacho-Tauta et al. [8] as well as Godlewski and Szczepański [18] were used. Generated vibrations had a frequency of less than 4 kHz. Thanks to that, the ratio of sample height to wave length L/λ was higher than 3 [18], which allowed to eliminate factors that might have affected the results. For the analysis of the signal, visual interpretation was used, using a method described as „major first peak” by Lee and Santamarina [28]. Additionally, low-pass filter was used with the frequency of 10 kHz, which helped with the removal of the noise. More details about the procedure and some aspects of measurement were described by Witowski [62]. The basic statistical information concerning selected parameters of the tested soils are presented in table 1. More detailed characteristic and statistical distributions for analyzed soils were presented by Bogusz and Witowski [7]. The tests were conducted at the confining pressures between 15 kPa to 2000 kPa, with most data is range from 100 up to 500 kPa.

Table 2. Summary of basic properties for analyzed soils a) clays; b) glacial tills [7].

Statistical parameters	Moisture content		Initial void ratio		Plasticity index		Liquidity index		Volume density		Initial shear modulus	
	w_c [%]		e_0 [-]		I_p [%]		I_L [%]		ρ [Mg/m ³]		G_0 [MPa]	
	a)	b)	a)	b)	a)	b)	a)	b)	a)	b)	a)	b)
Min	16,80	8,57	0,44	0,23	34,7 6	10,2 2	-0,12	-0,07	1,93	2,01	44,54	45,90
Max	30,82	20,08	0,82	0,54	140, 4	25,6 9	-0,01	0,41	2,15	2,38	217,7	592,5
Arithmetic average	20,71	13,21	0,57	0,37	55,3 9	15,0 8	-0,06	0,19	2,06	2,20	119,1	185,1
Standard deviation	4,37	2,69	0,10	0,06	30,7 4	3,69	0,04	0,12	0,06	0,07	47,62	114,9
CoV [%]	21,1	20,4	17,9	16,2	55,5	24,5	-58,7	63,2	3,08	3,18	40,0	62,1

3. RESULTS

3.1. RESULTS FROM SDMT

The presented data offer the first correlation of this type for soils in Poland. The SDMT method was validated by surface geophysical methods (CSWS and SASW) [18, [19]. New correlation relationships have been examined for typical soils present in Poland, for which the possibility of estimation of initial shear modulus G_0 was investigated on the basis of the standard results from DMT tests. The amount of data is already statistically significant in some cases (e.g. sands); however, the coherence of the results is still below the level for the relation to be meaningful. The observed scatter undoubtedly originates from the variability and diversity of the studied material. These results correspond well with the distribution of G_0/M_{DMT} versus K_D (fig.4). The graph presents the results from chosen tests sites and soil types, and the results confirm the facts given in Marchetti et al., [34]. Obtained correlations present various levels of reliability. Nonetheless, presented equations for glacial tills, clays, and sand, can be used in practice for prediction of the stiffness degradation curve.

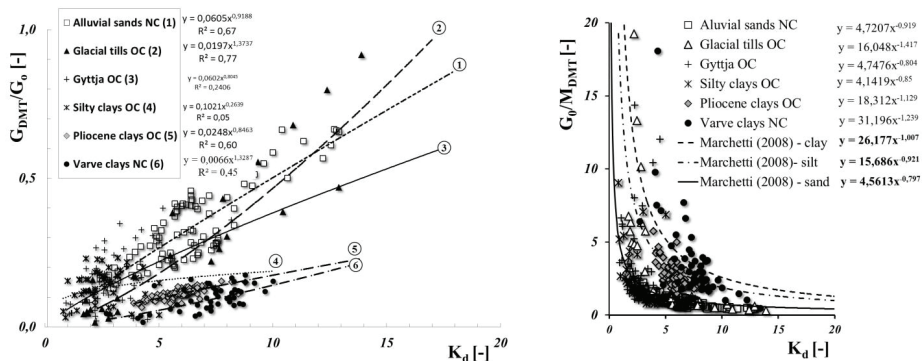


Fig. 4. Graph of the G_{DMT}/G_0 (left) and G_0/M_{DMT} indicator (right) vs K_D for chosen types of soils [18] with modifications.

3.2. RESULTS FROM LABORATORY TESTS

The presentation and the analysis of the results contained in the database of laboratory test results has been limited mainly to two soil types which were investigated, namely: “Pliocene” clays and glacial tills. Glaciation processes have been responsible for significant overconsolidation of those soils, observed now in OCR with typical values of 8–12 up to 50 (for Warsaw clays) []. The obtained results from all tests (laboratory and in situ) were summarized in graphs (Fig. 5).

Those graphs show that results from laboratory tests for OC clays and glacial tills are separated due to different shape of a normalized degradation curve (in function $G/G_0-\gamma$). Results obtained for glacial tills exhibit larger scatter of degradation range than clays. This situation is typical for this type of soil because of its natural variability.

In order to construct the $G-\gamma$ degradation curve, it is necessary to locate the *working strain* modulus G_{DMT} . In other words, it is necessary to know, at least approximately, the shear strain corresponding to G_{DMT} . Indications by Mayne [36] locate the DMT modulus (M_{DMT}) for sands at an intermediate level of strain ($\gamma \approx 0.05$ – 0.1%). Similarly Ishihara (after [2]) classified the DMT within the group of methods of measurement of soil deformation characteristics involving also an intermediate strain level (0.01 – 1%). More recent studies [2], [23] clearly showed that the working strain modulus depends on the soil texture: typical working strain ranges of G_{DMT} can be approximately assumed as 0.01 – 0.45% in sand, 0.1 – 2% in silt and clay, while higher than 2% in soft clay.

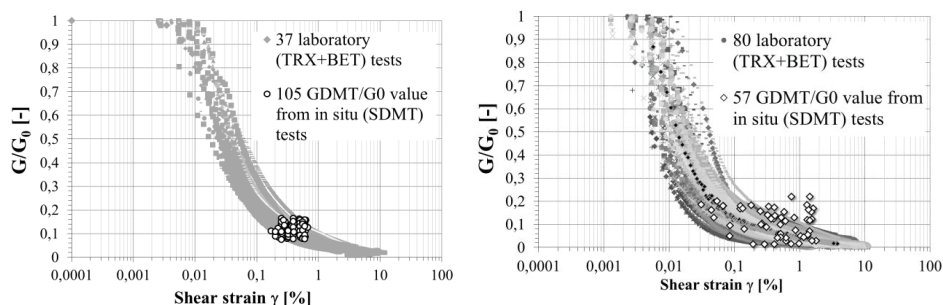


Fig. 5. Shape of the normalized G/G_0 - γ degradation curve's range and values of G_{DMT}/G_0 - γ_{DMT} based on the SDMT for OC clays (on left) and OC glacial tills (on right).

Next for estimating the shear strain the SDMT data obtained at the same depth were used. Based on M_{DMT} and using constitutional Eq. (1.12), a working strain modulus G_{DMT} was derived. For both types of soils, the estimated values of Poisson's coefficient from laboratory tests, were chosen as an average (0.3). Also for obtaining a normalized value, a small strain value G_0 was derived from V_s . After that, the horizontal ordinate line was superimposed to the same depth on proposed reference stiffness degradation curve. The intersection of the G_{DMT}/G_0 value provides a shear strain value referred as γ_{DMT} . Information about the stiffness at small strains (G_0) and the value of shear modulus at specific shear strain provides two points through which an interpolation of the data from the laboratory can be made in order to get the complete in-situ degradation curve G - γ . The values of the normalized working shear strain modulus ratio G_{DMT}/G_0 range from 0.08 to 0.16 in clays and 0.01 to 0.2 in glacial tills, while the range of values of the shear strain γ_{DMT} are 0.2% to 0.6% in clays, 0.04% to 1.8% in silty, sandy stiff clays (tills). Those results show that in OC soils, faster increase in stiffness with stress level and faster reduction in stiffness with strain level is visible than for typical NC, soft soils. These observations are in agreement with preliminary literature indications [31], [34], [44], [23], [52], [58].

4. EVALUATION OF IN SITU STIFFNESS DEGRADATION CURVE

The present paper aims to provide some recommendations for the interpretation of the results from in situ tests used in Polish practice (SDMT) for estimating the G - γ degradation curves for various type of soils. According to this procedure, if one were to define the in situ degradation curve, a reference strain level has therefore to be assigned. An alternative approach proposed here is to assign the shear

strain level and estimate shear strain stiffness, at that level, starting from SDMT results. The non-linear stress–strain behavior of soils at small to medium strains is mostly represented by some form of hyperbolic stress–strain relationship [13], [20], [56], [59]. After Darendeli [10], the best-fit functional relationship for the secant shear modulus degradation data as a modified hyperbolic equation takes the form:

$$(4.1) \quad \frac{G}{G_0} = \frac{1}{1 + \left(\frac{\gamma - \gamma_e}{\gamma_r} \right)^a}$$

where:

G – the secant shear modulus at any strain (γ), γ_r – reference strain value at which $G/G_0 = 0,50$, γ_e – elastic threshold strain beyond which the shear modulus falls below maximum, a – curvature parameter

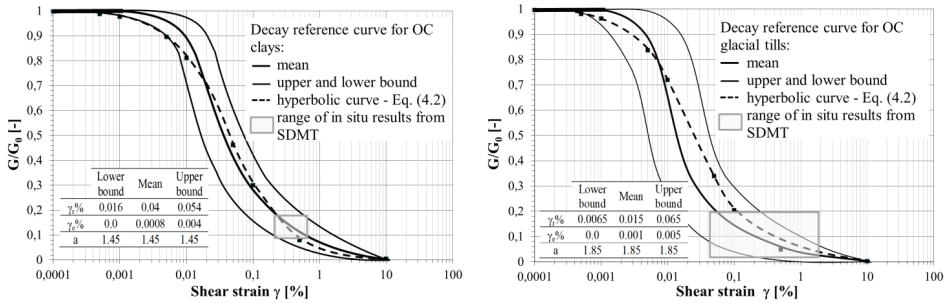


Fig. 6. Reference stiffness degradation curve for OC soils (for clays on left and glacial tills on right) and range of in situ results from SDMT.

Correction of this equation (after Bolton [56]) including γ_e as an additional curve-fitting parameter, is very useful because it helps to cover cementation and interlocking effects at small strains. For obtained datasets (clays and tills), stiffness degradation curves were established (fig. 6). Based on all results, average curve with upper- and lower-boundary was established. Parameters of the obtained curves, based on the equation (4.1) are presented.

Those models, with the implemented procedure (fig. 7) and established relationships, allow for evaluation of soil behaviour, based on in situ tests, at full range of deformations. At fig. 6, additional validation of those models was presented. This shear strain stiffness could be estimated by defining

the relation between G_{DMT} and the Dilatometer Modulus. The one of SDMT data determined at the investigated test sites was used to assist the construction of a hyperbolic stress-strain equation [2]:

$$(4.2) \quad \frac{G}{G_0} = \frac{1}{1 + \left(\frac{G_0}{G_{DMT}} - 1 \right) \frac{\gamma}{\gamma_{DMT}}}$$

The ratio G_{DMT}/G_0 obtained from SDMT and the estimated shear strain γ_{DMT} were used to plot the corresponding hyperbolic curve at one of test sites (typical for analyzed clays and glacial tills). The curves obtained from SDMT, using Eq. (4.2), presented on graph (black dash lines in Fig. 6) provide a reasonable fit to the proposed models (reference stiffness degradation curves). Based on the conducted analysis, as a summary, a proposal of a procedure is presented for evaluating stiffness characteristic based on in situ tests (fig. 7).

The diagram presents subsequent steps of the proposed method, depending on the availability of the test methods and their results. In the step I, when evaluating the stiffness degradation model, the use of DMT and SDMT with additional reference curves is preferred. Alternatively, the use of CPT with validated regional correlations (step II) can be used to obtain necessary stiffness parameters (G_{DMT}). Next stage (step VI) regard estimation of G_0 (based on seismic tests with V_s measurements). The points of the reference curve can be chosen using these data. Characterizing the stiffness of each ground requires the use of databases and establishing degradation models (step VI). With lack of such data, direct laboratory measurements can be used (step V). However, due to variability of most soils and usually very limited number of laboratory tests, this approach may not be representative. In such case, reference to data available in the literature is recommended. Last stage (step VII) is related to fitting of the typical shape (reference typical-shape from laboratory G - γ curves) using established two parameters (G_0 and G_{DMT}/G_0). Locating the second point on the G - γ curve is the main issue.

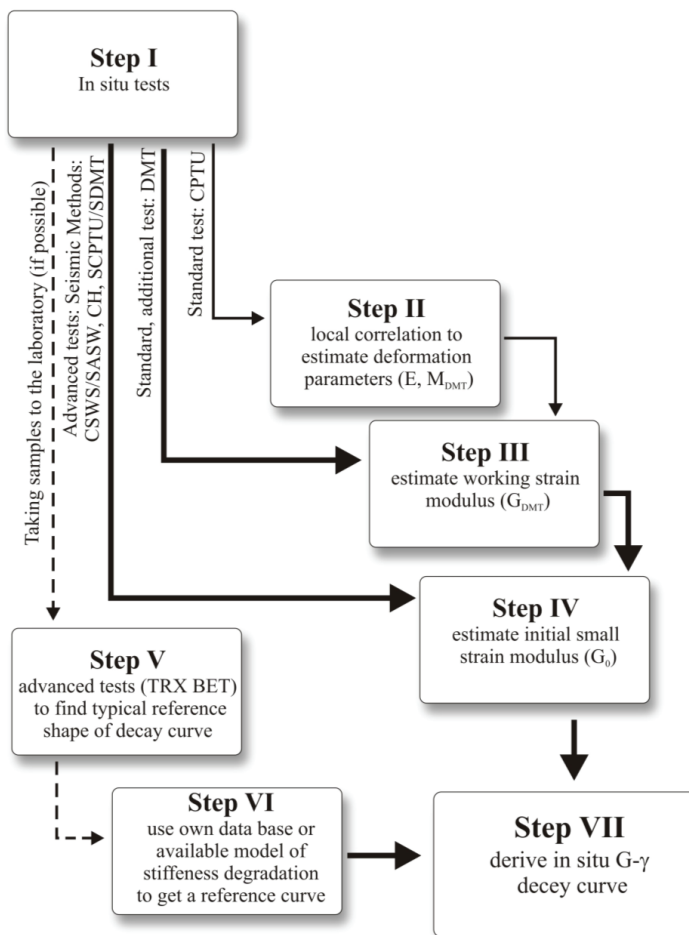


Fig. 7. Proposition of the procedure of evaluation of stiffness degradation curves from in situ tests.

It is necessary to know (at least approximately) the shear strain γ_{DMT} corresponding to working strain modulus G_{DMT} . Typical ranges of γ_{DMT} in different soil types could be inferred from the “intersection” of the SDMT data points with same-depth reference stiffness degradation curves – back-analyzed from the observed field behaviour under full-scale loading, or obtained by cyclic/dynamic laboratory tests, or reconstructed by the combined use of different in situ/laboratory techniques - at various test sites.

5. CONCLUSION

The development of interpretation methods of soundings is based mainly on statistical correlations which demand huge sets of measurements. The correlations between sounding results and geotechnical parameters require good regional determination or adaptation for local conditions. The results presented in this paper support the possible use of the CPTU, DMT and SDMT to assess the degradation of in situ stiffness with increase of strain level. This potential stems from the ability of the SDMT to provide routinely, at each test depth, both a small strain stiffness (G_0 from V_s) and a working strain stiffness G_{DMT} (derived via standard DMT correlations).

Presented results have high statistical value – approx. 3000 data points were used for the analysis of CPTU/DMT correlation, about 300 results from SDMT profiles, and about 130 laboratory tests (curves) to estimate reference shapes of degradation curves. Of course, it is recognized that given values require consideration of additional factors, accounting for uncertainty in correlation parameters. Especially, in the case of overconsolidated soils, the impact of stress history plays an important role on evaluation of stiffness characteristic [27], [29]. Some aspects and methodology associated with evaluation of overconsolidated soils (in Polish conditions) can be found in works of Wierzbicki [61].

The correlations presented in the article are based of solutions from the literature, therefore widely recognized and already applied in practice, but with additional considerations for local experience so they may be used in the Polish practice with less uncertainty.

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OCENA DEGRADACJI SZTYWNOŚCI Z BADAŃ POLOWYCH DLA RÓŻNYCH TYPÓW GRUNTÓW

Słowa kluczowe: sztywność gruntu, badania polowe (in situ), referencyjne krzywe degradacji sztywności, dylatometr sejsmiczny, grunty przekonsolidowane.

STRESZCZENIE

Coraz bardziej skomplikowane układy konstrukcyjne wymagają indywidualnego podejścia przy wyznaczaniu parametrów, za każdym razem uwzględniając i modelując już na etapie badań, późniejsze warunki współpracy z podłożem. Jak wykazały dane z literatury tematu oraz wyniki uzyskane z badań własnych, grunty charakteryzują się silną nieliniowością modułu w zależności od odkształcenia, zatem należy precyzyjnie dobierać metody badania podłoża, tzn. w zakresie ich „czułości” pomiarowej, odpowiedniej dla danego typu konstrukcji budowlanych. Gdy nie są dostępne bezpośrednie pomiary, a metoda obliczeń projektowych wymaga określonych parametrów, wtedy rozwiązaniem pomocnym staje się poszukiwanie zależności korelacyjnych z poligonów badawczych i stosowanie procedur pozwalających na oszacowanie wymaganych parametrów (przy najmniej na etapie początkowych analiz). W artykule przedstawiono schematu postępowania w zakresie opisu i oceny sztywności podłoża na podstawie badań polowych (CPTU, DMT i SDMT) i opracowanych krzywych referencyjnych z badań laboratoryjnych (TRX) dla wybranych typów gruntów (iły i gliny). W oparciu o podany algorytm możliwe jest wyznaczenie wartości modułu G_0 dla dowolnej wielkości strefy odkształcenia, stosując uzyskane z badań własnych zależności lokalne, w tym modele degradacji podłoża.